## Action Recognition

## Approaches

- FSA
- HMMs/NNs
- Rule-based
- Representation is important


## FSA: Hand Gesture Recognition



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## FSA: Hand Gesture Recognition



## Hunt events



## FSA: Recognizing Human Behavior in Office Environment



## Rule-Based: Detecting Violence



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## Rule-Based: Detecting Violence



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## Rule-Based: Recognizing Outdoor Activities



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## Limitations

- A priori knowledge
- Extensive training
- No explanation
- No learning
- Representation
- View invariance


## View-invariant Representation and Recognition of <br> Human Action

## Hand Actions Recognition

- hand generates a 3-D trajectory with respect to time.
- analyze 2-D projection of this 3-D trajectory.
- View invariance issues.


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## Hand Actions



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## Spatiotemporal Curve

$$
r_{s t}=\left[\begin{array}{lll}
x(t) & y(t) & t
\end{array}\right]
$$



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## Spatiotemporal Curvature

$$
k=\frac{\sqrt{A^{2}+B^{2}+C^{2}}}{(, .)^{2}} \quad A=\left|\begin{array}{ll}
y^{\prime} & t^{\prime} \\
y^{\prime \prime} & t^{\prime \prime}
\end{array}\right|, B=\left|\begin{array}{ll}
t^{\prime} & x^{\prime} \\
t^{\prime \prime} & x^{\prime \prime}
\end{array}\right|, C=\left|\begin{array}{ll}
x^{\prime} & y^{\prime} \\
x^{\prime \prime} & y^{\prime \prime}
\end{array}\right|
$$

Spatiotemporal curvature captures both the speed and direction changes in one quantity.

## Representation of Actions

- Dynamic Instants:
- Maximum in spatiotemporal curvature represents an important change of motion characteristic.
- Intervals


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## Action Units

- Psychology research shows:
- People tend to divide an action into atomic units at the places where the motion characteristics change the most.
- Stops, starts, pauses, dynamic instants


## Viewing Directions and Spatiotemporal Curvature




Although the viewing directions are quite different, the peak locations are consistent.

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## View-invariant Matching

- Consider 3D trajectories as 3D objects.


## Action Trajectory in 4D



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 direction


2D trajectory 2D trajectory

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## Affine View Invariant Matching

## RankTheorem_(Tomasi\&KKanade)

- $S$ is a set of 3-D points and $\Pi$ s are projection matrices for different viewpoints, then we can arrange image coordinates of points in an observation matrix, M, as follows:

$$
\begin{array}{r}
M=\left[\begin{array}{llll}
\mu_{1}^{v_{1}} & \mu_{2}^{v_{1}} & \ldots & \mu_{n}^{v_{1}} \\
v_{1}^{v_{1}} & v_{2}^{v_{1}} & \ldots & v_{n}^{v_{1}} \\
\mu_{1}^{v_{2}} & \mu_{2}^{v_{2}} & \ldots & \mu_{n}^{v_{2}} \\
v_{1}^{v_{2}} & v_{2}^{v_{2}} & \ldots & v_{n}^{v_{2}}
\end{array}\right]=P \bullet S=\left[\begin{array}{lll}
\Pi_{v_{1}} \\
\Pi_{v_{2}}
\end{array}\right] \bullet\left[\begin{array}{ccc}
X_{1} & X_{2} & X_{n} \\
Y_{1} & Y_{2} & \cdots \\
Z_{n} \\
Z_{1} & Z_{2} & Z_{n}
\end{array}\right] \\
\Pi_{v}=\left[\begin{array}{lll}
a_{1} & a_{2} & a_{3} \\
a_{4} & a_{5} & a_{6}
\end{array}\right]
\end{array}
$$

$M$ is 4 by $n, P$ is $4 \times 3$ and $S$ is $3 \times n$, then the rank of M is at most 3 .

## Generalized Affine Rank Theorem

- A set of image points match if and only if M is of rank at most 3. (Shapiro \& Zisserman, Seitz \& Dyer)
- A set of "instants" match if and only if M of rank at most 3 . Therefore, the similarity measure is:

$$
M=\left[\begin{array}{cccc}
\mu_{1}^{i} & \mu_{2}^{i} & \ldots & \mu_{n}^{i} \\
v_{1}^{i} & v_{2}^{i} & \ldots & v_{n}^{i} \\
\mu_{1}^{j} & \mu_{2}^{j} & \ldots & \mu_{n}^{j} \\
v_{1}{ }^{j} & v_{2}^{j} & \ldots & v_{n}^{j}
\end{array}\right] \quad \operatorname{dist}_{i, j}=\left|\sigma_{4}\right|
$$

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- Fundamental matrix captures the relationship between the corresponding points in two views.

$$
\left[\begin{array}{c}
u_{i} \\
v_{i} \\
1
\end{array}\right]^{T} F\left[\begin{array}{c}
u_{i}^{\prime} \\
v_{i}^{\prime} \\
1
\end{array}\right]=0, \quad F=\left[\begin{array}{lll}
f_{11} & f_{12} & f_{13} \\
f_{21} & f_{22} & f_{23} \\
f_{31} & f_{32} & f_{33}
\end{array}\right]
$$

## Perspective View-imvoriont

## Mieasurre

- Consider the fundamental matrix constraint and rearrange the constraint as following:

$$
\left[\begin{array}{c}
u_{i} \\
v_{i} \\
1
\end{array}\right]^{T} F\left[\begin{array}{c}
u_{i}^{\prime} \\
v_{i}^{\prime} \\
1
\end{array}\right]=0,
$$

$$
M f=\left[\begin{array}{ccccccccc}
u^{\prime} u_{1} & u_{1}^{\prime} v_{1} & u_{1}^{\prime} & v_{1}^{\prime} u_{1} & v_{1}^{\prime} v_{1} & v_{1} & u_{1} & v_{1} & 1 \\
u^{\prime} u_{2} & u_{2}^{\prime} v_{2} & u_{2}^{\prime} & v_{2}^{\prime} u_{2} & v_{2}^{\prime} v_{2} & v_{2}^{\prime} & u_{2} & v_{2} & \\
\vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\
u_{n}^{\prime} u_{n} & u_{n}^{\prime} v_{n}^{\prime} & u_{n}^{\prime} & v_{n}^{\prime} u_{n} & v_{n}^{\prime} v_{n} & v_{n}^{\prime} & u_{n} & v_{n} & 1
\end{array}\right] f=0
$$

M is 9 by $n$ matrix $\quad f=\left[\begin{array}{lllllllll}f_{11} & f_{12} & f_{13} & f_{21} & f_{22} & f_{23} & f_{31} & f_{32} & f_{33}\end{array}\right]$

To solve the equation, the $\operatorname{rank}(\mathrm{M})$ must be 8 . The $9^{\text {th }}$ singular value of $\mathrm{M}, \sigma_{9}$, is the match measure.

## Instant-Interval Representation

- We have not used the interval information
- View Invariance
- Temporal Invariance


## DTW and Temporal Signals

- Match two 1 D temporal signals:

- Match two 2D temporal curves:



## Warping

$$
\begin{aligned}
A & =\left[a_{1}, a_{2}, \ldots, a_{i}, a_{I}\right] \\
B & =\left[b_{1}, b_{2}, \ldots, b_{j}, b_{J}\right] \\
d_{i j}= & =\left|a_{i}-b_{j}\right| \\
g_{11} & =2 d_{11}
\end{aligned}
$$

$$
g(i, j)=\min \left[\begin{array}{c}
g(i-1, j-2)+2 d(i, j-1)+d(i, j) \\
g(i-1, j-1)+2 d(i, j) \\
g(i-2, j-1)+2 d(i-1, j)+d(i, j)
\end{array}\right]
$$

## Affine View-invariant DTW

Step 1: Pick up 4 instants from trajectories $I$ and $I^{\prime},\left(x_{1} y_{1}\right)$, $\left(x_{22} y_{2}\right),\left(x_{2} y_{3}\right),\left(x_{42} y_{4}\right)$ and $\left(x_{1}^{\prime} y_{1}\right),\left(x_{2}^{\prime} y_{2}\right),\left(x_{3}^{\prime} y_{3}^{\prime}\right),\left(x_{4}^{\prime} y_{4}^{\prime}\right)$ are image coordinates.
Step 2: Apply Dynamic Time Warping

- the similarity between $i^{i^{\text {h }}}\left(u_{i j} v_{i}\right)$ and $j^{\text {th }}\left(u_{j}^{\prime} v_{j}^{\prime}\right)$ point is:

$$
d(i, j)=\left|\sigma_{4}\right| \quad M=\left[\begin{array}{lllll}
x_{1} & x_{2} & x_{3} & x_{4} & u_{i} \\
y_{1} & y_{2} & y_{3} & y_{4} & v_{i} \\
x_{1}^{\prime} & x_{2}^{\prime} & x_{3}^{\prime} & x_{4}^{\prime} & u_{j}^{\prime} \\
y_{1}^{\prime} & y_{2}^{\prime} & y_{3}^{\prime} & y_{4}^{\prime} & v_{j}^{\prime}
\end{array}\right]
$$

## Affine View-invariant DTW (Con.)

Step 3: if there are more than 4 pairs of instants in the trajectories, go back to step 1 and try other combinations of 4 instants.

Step 4: pick the minimal matching error as the similarity measurement and get the correspondence result.

## Matching using View-invariant Dynamic Time Warping

Step 1) Pick up 4 instants from each of trajectory

Step 2) DTW using the view invariant similarity measure, $\sigma 4$, for intervals


Step 4) get the minimum similarity measurement and correspondence result

## Action Recognition Results



Difference $=2$


Difference $=2.3$

## Action Recognition Results



Difference $=2.5$


Difference $=3.2$

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## View-invariant DTW Results



Difference $=2.3$


Difference $=71$

## Experimental Results

## 60 Action Trajectories 7 People

| 8 | 7 | 3 |  |  |  | $\rightarrow$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | \% | 1 | \% | $\checkmark$ | 8 |  |  | 7 |  |  |  |
| 7 |  |  | 8 | 7 |  |  | 7 | $\rangle$ | 8 |  |  |
| 9. | $\square$ | 8 | 5 |  | T. | 8 | $\bigcirc$ | 8 | 5 | \% | , $>$ |
| r. | $\checkmark$ | $\checkmark$ | 7 | $\zeta$ | 3. |  | 3 | 5 | . | $\checkmark$ | . |

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## Experimental Results

| Actions | 3 Best matches | Evaluation \& comments |
| :--- | :--- | :--- |
| 1 | 294338 | Correct |
| 2 | Pick up | Correct |
| 3 | 18236 | Correct |
| 4 | 11416 | One wrong |
| 5 |  | Unique action |
| 6 | 18323 | Correct |
| 7 | 48338 | correct |
| 8 | 48337 | One wrong |
| 9 | Pick up | Correct |
| 10 | Put down | Correct |
| 11 | Pick up | Correct |
| 12 | Put down | Correct |
| 13 |  | Unique action |
| 14 | 43161 | Correct |
| 15 |  | Unique action |
| 16 | 14291 | Correct |
| 17 | Pick up | Incorrect, object hidden |
| 18 | 6323 | Correct |
| 19 | Pick up | Correct |
| 20 |  | Unique random motion |

## Temporal Alignment of Videos



Trajectories of the right foot:
Input videos: Copyright Mubarak Shah 2003

## Temporal Alignment Results

Synchronized videos:


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## Temporal Alignment Results

Before Temporal Alignment


After Temporal Alignment


## Temporal Alignment Results

Non-overlapping video temporal alignment:


Left Seq



Right Seq



Histogram of Misalignment


- Cen Rao, Alexei Gritai, Mubarak Shah, View-invariant Alignment and Matching of Video Sequences. The Ninth IEEE International Conference on Computer Vision, Nice, France, 2003.
Project web page.
- Cen Rao, Alper Yilmaz, Mubarak Shah. View-Invariant Representation And Recognition of Actions, International Journal of Computer Vision, Vol. 50, Issue 2, 2002.


## Anthropometric Representation for Invariant Action Recognition



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## Representation of Actors



- Point-based modeI contains sufficient description for the recognition of human actions, [1].
[1] G. Johanasson. Visual perception of biological motion and a model for its analysis. Perception and Psychophysics, 14(2): 201 - 211, 1993.


## Anthropometry

- \An`thro*pom"e*try<br>, $n$. Measurement of the height and other dimensions of human beings, especially at different ages, or in different races, occupations, etc.
- Variability in human proportion is not arbitrary.
- Action Recognition must address this variation.


## Pose and Posture

- Posture: The stance an actor has at a time instant
- Pose: The global orientation and position of an actor



## Anthropometric Constraint

- Conjecture: The relationship between points of two actors X and Y in the same posture can be described by a matrix M

$$
\mathbf{X}_{i}=M \mathbf{Y}_{i}
$$

where $\mathrm{i}=1,2 \ldots n, M$ is a 4 x 4 non-singular matrix, $\mathbf{X}_{i}$ and $\mathbf{Y}_{i}$ are sets of points describing two actors.

- This transformation simultaneously captures:
- the different poses
- difference in size/proportions.


## Anthropometric Constraint

- This was verified empirically between the $5^{\text {th }}$ percentile woman and $95^{\text {th }}$ percentile man.
- Mean error of
- 227.3 mm before the transformation,
- 23.87 mm after the transformation.
R. Bridger. Human Performance Engineering: A Guide for system designers, Prentice Hall, 1982

| Dimension | Men |  |  |  | Women |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 5th \%ile | 50th \%ile | 95th \%ile | SD | 5th \%ile | 50th \%ile | 95th \%ile | SD |
| 1. Stature | 1625 | 1740 | 1855 | 70 | 1505 | 1610 | 1710 | 62 |
| 2. Eye height | 1515 | 1630 | 1745 | 69 | 1405 | 1505 | 1610 | 61 |
| 3. Shoulder height | 1315 | 1425 | 1535 | 66 | 1215 | 1310 | 1405 | 58 |
| 4. Elbow height | 1005 | 1090 | 1180 | 52 | 930 | 1005 | 1085 | 46 |
| 5. Hip height | 840 | 920 | 1000 | 50 | 740 | 810 | 885 | 43 |
| 6. Knuckle height | 690 | 755 | 825 | 41 | 660 | 720 | 780 | 36 |
| 7. Fingertip height | 590 | 655 | 720 | 38 | 560 | 625 | 685 | 38 |
| 8. Sitting height | 850 | 910 | 965 | 36 | 795 | 850 | 910 | 35 |
| 9. Sitting eye height | 735 | 790 | 845 | 35 | 685 | 740 | 795 | 33 |
| 10. Sitting shoulder height | 540 | 595 | 645 | 32 | 505 | 555 | 610 | 31 |
| 11. Sitting elbow height | 195 | 245 | 295 | 31 | 185 | 235 | 280 | 29 |
| 12. Thigh thickness | 135 | 160 | 185 | 15 | 125 | 155 | 180 | 17 |
| 13. Buttock-knee length | 540 | 595 | 645 | 31 | 520 | 570 | 620 | 30 |
| 14. Buttock-poplitasil length | 440 | 495 | 550 | 32 | 435 | 480 | 530 | 30 |
| 15. Knee height | 490 | 545 | 595 | 32 | 455 | 500 | 540 | 27 |
| 16. Popliteal height | 395 | 440 | 490 | 29 | 355 | 400 | 445 | 27 |
| 17. Shoulder breadth (bideltoid) | 420 | 465 | 510 | 28 | 355 | 395 | 435 | 24 |
| 18. Shoulder breadth (biacromial) | 365 | 400 | 430 | 20 | 325 | 355 | 385 | 18 |
| 19. Hip breadth | 310 | 360 | 405 | 29 | 310 | 370 | 435 | 38 |
| 20. Chest (bust) depth | 215 | 250 | 285 | 22 | 210 | 250 | 295 | 27 |
| 21. Abdominal depth | 220 | 270 | 325 | 32 | 205 | 255 | 305 | 30 |
| 22. Shoulder-elbow length | 330 | 365 | 395 | 20 | 300 | 330 | 360 | 17 |
| 23. Elbow-fingertip length | 440 | 475 | 510 | 21 | 400 | 430 | 460 | 19 |
| 24. Upper limb length | 720 | 780 | 840 | 36 | 655 | 705 | 760 | 32 |
| 25. Shoulder-grip length | 610 | 665 | 715 | 32 | 555 | 600 | 650 | 29 |
| 26. Head length | 180 | 195 | 205 | 8 | 165 | 180 | 190 | 7 |
| 27. Head breadth | 145 | 155 | 165 | 6 | 135 | 145 | 150 | 6 |
| 28. Hand length | 175 | 190 | 205 | 10 | 160 | 175 | 190 | 9 |
| 29. Hand breadth | 80 | 85 | 95 | 5 | 70 | 75 | 85 | 4 |
| 30. Foot length | 240 | 265 | 285 | 14 | 215 | 235 | 255 | 12 |
| 31. Foot breadth | 85 | 95 | 110 | 6 | 80 | 90 | 100 | 6 |
| 32. Span | 1655 | 1790 | 1925 | 83 | 1490 | 1605 | 1725 | 71 |
| 33. Elbow span | 865 | 945 | 1020 | 47 | 780 | 850 | 920 | 43 |
| 34. Vertical grip reach (standing) | 1925 | 2060 | 2190 | 80 | 1790 | 1905 | 2020 | 71 |
| 35. Vertical grip reach (sitting) | 1145 | 1245 | 1340 | 60 | 1060 | 1150 | 1235 | 53 |
| 36. Forward grip reach | 720 | 780 | 835 | 34 | 650 | 705 | 755 | 31 |

## Postural Constraint

- Proposition 1: If $x_{t}$ and $y_{t}$ describe the imaged posture of two actors at time $t$, a Fundamental Matrix can be uniquely associated with $\left(\mathbf{x}_{t}, \mathbf{y}_{t}\right)$ if the two actors are in the same posture.

$$
x_{t}^{T} \Gamma y_{t}=0
$$

$\square$ Two actors performing the action instead of two views.
$\square$ This is valid for a single time instance.

## Postural Constraint

- The similarity of posture between two actors can be measured using the ninth singular value of a measurement matrix $A$, where $A f=0$.

$$
\left[\begin{array}{ccc}
x_{1}^{\prime} x_{1} & \ldots & x_{n}^{\prime} x_{n} \\
x_{1}^{\prime} y_{1} & \ldots & x_{n}^{\prime} y_{n}^{\prime} \\
x_{1}^{\prime} & \ldots & x_{n}^{\prime} \\
y_{1}^{\prime} x_{1} & \ldots & y_{n}^{\prime} x_{n} \\
y_{1}^{\prime} y_{1} & \ldots & y_{n}^{\prime} y_{n} \\
y_{1}^{\prime} & \ldots & y_{n}^{\prime} \\
x_{1} & \ldots & x_{n} \\
y_{1} & \ldots & y_{n} \\
1 & \ldots & 1
\end{array}\right]\left[\begin{array}{l}
F_{11} \\
F_{12} \\
F_{13} \\
F_{21} \\
F_{22} \\
F_{23} \\
F_{31} \\
F_{32} \\
F_{33}
\end{array}\right]=A f=0
$$

## Capturing View Variance

- The fundamental matrix captures the variability in proportion as well as the change in view.



## Action Constraint

- Proposition 2: For an action element $\mathbf{u}_{t}$, the fundamental matrices associated with ( $\mathrm{x}_{t}, \mathrm{y}_{t}$ ) and $\left(\mathrm{x}_{t+1}, \mathrm{y}_{t+1}\right)$ are the same if both actors perform the action element defined by $\mathbf{u}_{t}$.



## Measuring Action Similarity

- Since all the Fs are the same:

$$
\begin{aligned}
& A_{1} f=0 \\
& A_{2} f=0 \\
& \vdots \\
& A_{k} f=0
\end{aligned}
$$

- Thus the ninth singular value of

$$
\boldsymbol{A}=\left[A_{1}, A_{2} \ldots A_{k}\right]
$$

can be used as a view invariant measure.

## Experimental Results

- We performed a diverse set of experiments
- Action Detection
- Analyzing periodicity
- Multiple view multiple people
- Action Synchronization
- Following the leader
- Odd one out


## Action Detection

Analyzing Periodicity


## Action Detection

Analyzing Periodicity


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## Action Detection:

## Different approaches, different people, the same action



ReferencePattern


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## Action Detection:

## Different approaches, different people, the same action



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## Analyzing Actions Odd One Out



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## 'Odd One Out'



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## Action Synchronization Following the Leader



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## Action Synchronization Following the Leader



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