

Fall 2019 CIS 3362 Week One Assignment Solutions

1) It's easy enough to write a program which takes in the input and outputs the input shifted by the 26 possible shifts. When we run the attached program (hmk1-12.c), we see that adding 12 to the cipher text produces the following plain text (I've added spaces and punctuation):

```
This is just the first question. Don't be thrown off by the
appearance of a q.
```

The corresponding encryption key was $k = 14$, since the decryption key, $+12 \equiv -14 \pmod{26}$.

2) Run the same program on the ciphertext given. When we add 19 to the ciphertext, we get the following plaintext:

```
It was the best of times. It was the worst of times.
```

The corresponding encryption key was $k = 7$, since the decryption key, $+19 \equiv -7 \pmod{26}$.

2) Now, run a program that tries all 312 possible affine cipher keys on the ciphertext to see which produces meaningful output. The attached program (hmk1-34.c) does this. After combing through the results, we find that applying $a = 19$, $b = 10$, the correct decryption keys, produces the following output

```
For this question you had to look through three hundred and twelve
possible decipherments. Hope you didn't get cross-eyed.
```

We can do the following math to find the corresponding encryption keys:

$$\begin{aligned}f(x) &= (19x + 10) \pmod{26} \\x &= (19f^{-1}(x) + 10) \pmod{26} \\(x - 10) &= 19f^{-1}(x) \pmod{26} \\11(x - 10) &= 11(19f^{-1}(x)) \pmod{26} \\f^{-1}(x) &= (11x - 110) \pmod{26} \\f^{-1}(x) &= (11x + 20) \pmod{26}\end{aligned}$$

Thus, the encryption keys were $a = 11$, $b = 20$.

4) Edit the code used for #3 to remove both loops, set $b = 19$ and $i = 6$ (since $ALIST[6] = 15$) and then run the program which produces the following cipher text:

```
ktxnrpivaljsuqjwbmvebgcjzhvoyhfd
```