

# AES (Advanced Encryption Standard)

DES - 56 bit key  $2^{56}$  keyspace

late 1990s - DES Challenge - distributed effort  
50ish days + key was found.

Made a competition for a new standard

- ① secure
- ② fast
- ③ simple

Winner: Rijndahl  
"rain doll"

\* 3 Versions: 128 bit version \*  
192 bit version  
256 bit version

Key drawn as a byte array of 16 bytes  
(8 bits)  
2HEXCHAR

State Matrix

$b_1$	$b_5$	$b_9$	$b_{13}$
$b_2$	$b_6$	$b_{10}$	$b_{14}$
$b_3$	$b_7$	$b_{11}$	$b_{15}$
$b_4$	$b_8$	$b_{12}$	$b_{16}$

- ① Add Round Key
- ② Sub Bytes
- ③ Shift Rows
- ④ Mix Columns

# Encrypt (10 ROUNDS)

10/7/19 (2)

- ① Plaintext
- ② Add Round Key (round 0 key)
- ③ RUN 9 FULL ROUNDS
- ④ RUN LAST ROUND ADJUSTED

## REG ROUND

- ① Sub bytes
- ② Shift rows
- ③ mix cols
- ④ Add Round Key

## ROUND 10

- ① Sub bytes
- ② Shift Rows
- ③ Add Round Key

## Sub bytes (S box)

Straight look up table -  
for each byte w/ sub it with  
another byte

## Shift Rows

$b_{00}$	$b_{01}$	$b_{02}$	$b_{03}$
$b_{10}$	$b_{11}$	$b_{12}$	$b_{13}$
$b_{20}$	$b_{21}$	$b_{22}$	$b_{23}$
$b_{30}$	$b_{31}$	$b_{32}$	$b_{33}$



$b_{00}$	$b_{01}$	$b_{02}$	$b_{03}$
$b_{11}$	$b_{12}$	$b_{13}$	$b_{10}$
$b_{22}$	$b_{23}$	$b_{20}$	$b_{21}$
$b_{33}$	$b_{30}$	$b_{31}$	$b_{32}$

# Mix Cols

10/7/19 (3)

Fixed matrix encryption + decryption

↓  
inverse of encryption

fixed!

State

$$\begin{bmatrix} 2 & 3 & 1 & 1 \\ 1 & 2 & 3 & 1 \\ 1 & 1 & 2 & 3 \\ 3 & 1 & 1 & 2 \end{bmatrix} \begin{bmatrix} 47 & B1 & 76 & 98 \\ 3A & C3 & 59 & BB \\ B2 & 72 & EA & D2 \\ FO & 19 & 03 & E3 \end{bmatrix}$$

Use the same "pattern" as matrix multiplication, but mult and add are done completely differently!

$$R_{1C1} = \underset{w}{2} \times \underset{i}{47} + 3 \times 3A + 1 \times B2 + 1 \times FO$$

All AES computations occur in the field  $GF_{2^8}$  with the irreducible polynomial  $x^8 + x^4 + x^3 + x + 1$ .

$$47 = 01000111 = x^6 + x^2 + x + 1$$

↑ ↑ ↑ ↑ ↑ ↑ ↑  
 $x^7 x^6 x^5 x^4 x^3 x^2 x^1 x^0$

$$3A = 00111010 = x^5 + x^4 + x^3 + x$$

$GF_{2^8}$  means a poly w/ max degree 7  
↑ all coeff  $\in \{0, 1\}$