

CIS 3362 Final Exam - Part B (Modern Private Key Cryptography) - 25 pts Solutions

1) (8 pts) Let the input to the S-boxes in DES be 8EF943C62DA1, represented in hexadecimal. What is the output from the S-boxes, represented in hex? (Your grade will be 1 point per hex character.)

Solution

Converting the input into 8 six bit blocks we get the following and then put them into the appropriate S boxes:

- $S_1(100011) = \text{row 3, col 1 entry of } S_1 = 12 \text{ (C)}$
- $S_2(101111) = \text{row 3, col 7 entry of } S_2 = 2 \text{ (2)}$
- $S_3(100101) = \text{row 3, col 2 entry of } S_3 = 13 \text{ (D)}$
- $S_4(000011) = \text{row 1, col 1 entry of } S_4 = 8 \text{ (8)}$
- $S_5(110001) = \text{row 3, col 8, entry of } S_5 = 6 \text{ (6)}$
- $S_6(100010) = \text{row 2, col 1, entry of } S_6 = 14 \text{ (E)}$
- $S_7(110110) = \text{row 2, col 11, entry of } S_7 = 8 \text{ (8)}$
- $S_8(100001) = \text{row 3, col 0, entry of } S_8 = 2 \text{ (2)}$

Output in HEX is **C2D86E82.**

Grading: 1 pt per HEX char no exceptions

2) (7 pts) What is the result of the multiplication $03 \times B6$, in the AES field? In order to get credit, you must show all of your work by hand.

Solution

$$03 \times B6 = 02 \times B6 + 01 \times B6$$

$$02 \times B6 = 1\ 0110\ 1100 \qquad 01 \times B6 = 1011\ 0110$$

$$\begin{array}{r} = 0110\ 1100 \\ + 1\ 1011 \\ \hline 0111\ 0111 \end{array}$$

$$\begin{array}{r} \text{Adding we get } 0111\ 0111 \\ + 1011\ 0110 \\ \hline \end{array}$$

1100 0001, in HEX we have **C1**.

Grading: 1 pt for listing out bits on $01 \times B6$, 4 pts for doing the $02 \times B6$ multiplication (1 pt for shift, 2 pts for 11011, 1 pt for answer), 2 pts for the final XOR.

3) (10 pts) The code included below has produced the following output:

Gpqef3Yx8/+0LTrq4nmlgrj

What was the string entered by the user that produced this output?

To answer the question, **you may run and edit this code as you see fit.** Alternatively, you may solve the problem by hand. There are reliable ways to do either but the former is almost definitely faster. Regardless of which method you choose, explain what you did and explain why it works.

Solution

What the code does is take the input, convert the regular ascii characters to their corresponding integer RADIX-64 values, XOR that integer with the position of the integer mod 64 (this is what `i&63` really does, it isolates the last 6 bits of the variable `i`, which is mathematically equivalent to mod 64). Then that resulting integer is converted back to its equivalent RADIX-64 character. Thus, this is like a block cipher with 6 bit blocks where each block is XORed with a fixed key based on the letter position. To undo an XOR, you just XOR it with the same value, since each bit will get canceled with itself in the second XOR, revealing the plaintext. So, it's good enough to run this same code, but enter in the ciphertext, to reveal the plaintext, which is:

Goodbye2020/Hello2020+1

Grading: 8 pts for the answer any which way, 2 pts for explaining that to undo an XOR, you just XOR with the same thing.

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>

char* makeCode(char* word);
char intToChar(int n);
int charToInt(char c);

int main(void) {
    char* ptr = malloc(25);
    scanf("%s", ptr);
    char* res = makeCode(ptr);
    printf("%s\n", res);
    free(ptr);
    free(res);
    return 0;
}

char* makeCode(char* word) {
    int n = strlen(word);
    char* res = malloc(sizeof(char)*(n+1));
    for (int i=0; i<n; i++)
        res[i] = intToChar(charToInt(word[i])^(i&63));
    res[n] = '\0';
    return res;
}
```

```
char intToChar(int n) {
    if (n < 26) return 'A'+n;
    if (n < 52) return 'a'+n-26;
    if (n < 62) return '0'+n-52;
    if (n == 62) return '+';
    return '/';
}

int charToInt(char c) {
    if (c >= 'A' && c <= 'Z') return c - 'A';
    if (c >= 'a' && c <= 'z') return c - 'a' + 26;
    if (c >= '0' && c <= '9') return c - '0' + 52;
    if (c == '+') return 62;
    return 63;
}
```