

Computer Science Department University of Central Florida

COP 3502 – Computer Science I

Announcements

■ Quiz 2 today

Available until 11:55 PM ■ You CANNOT go back on questions

- **Program 3 Due Wednesday**
- Exam 1 on Friday, 10/1/2010

Extensions on stuff?

■ Short answer: not gonna happen

Announcements

Comment on extension requests:

- \blacksquare # of hours expected of a full-time college student:
	- **Just like a full-time job: around 40 or 50 or so hours/week**
- **If is said that for every hour in class,**
	- **You can expect up to three hours of work outside class**
- Now do the math:
	- **If you are registered for 12 credits**
		- That adds up to 36 hours of outside-class work per week
		- **For a total of 48 hours per week**
- Now ask yourself:
	- For this class, do you really put in 9 hours/week outside of the class?

Announcements

Comment on extension requests:

- Now ask yourself:
	- For this class, do you really put in 9 hours/week outside of the class?
	- **Not even close!**
	- **If there's no program due, the average student puts in** ZERO hours per week outside class
		- **They don't even review notes for a MINUTE!**
	- So how long then does a program take?
		- **Let's even say 10 hours (which is high for most students)**
		- Since they are due every two weeks (or so)
		- That adds up to 5 hours per week that you invest (at a max)
	- Leaving still 4 hours per week of study time!

Big-O Notation

■ What is Big O?

Big O comes from Big-O Notation

- \blacksquare In C.S., we want to know how efficient an algorithm is…how "fast" it is
- More specifically...we want to know **how the performance of an algorithm responds to changes in problem size**
- The goal is to provide a *qualitative* insight on the # of operations for a problem size of *n* elements.
- \blacksquare And this total # of operations can be described with a mathematical expression in terms of *n*.
	- This expression is known as Big-O

- **Examples of Analyzing Code:**
	- We now go over many examples of code fragments
	- Each of these functions will be analyzed for their runtime in terms of the variable n
	- **Utilizing the idea of Big-O,**
		- **determine the Big-O running time of each**

- Example 1:
	- Determine the Big O running time of the following code fragment:

```
for (k = 1; k \le n/2; k++)sum = sum + 5;
}
for (j = 1; j \leq n*n; j++)delta = delta + 1;
}
```


- Example 1:
	- So look at what's going on in the code:
		- We care about the total number of REPETITIVE operations.
			- **Remember, we said we care about the running time for** LARGE values of n
			- So in a for loop with n as part of the comparison value **determining when to stop** | for (k=1; k<=n/2; k++)
			- Whatever is INSIDE that loop will be executed a LOT of times
			- **So we examine the code within this loop and see how** many operations we find
				- When we say operations, we're referring to mathematical operations such as +, -, *, /, etc.

Example 1:

- So look at what's going on in the code:
	- **The number of operations executed by these loops is** the sum of the individual loop operations.
	- We have 2 loops,
		- **The first loop runs n/2 times**
		- **Each iteration of the first loop results in one operation**
			- The + operation in: $sum = sum + 5$;
		- So there are n/2 operations in the first loop
		- The second loop runs n^2 times
		- Each iteration of the second loop results in one operation
			- The + operation in: delta = delta + 1;
		- So there are n² operations in the second loop.

Example 1:

- So look at what's going on in the code:
	- **The number of operations executed by these loops is** the sum of the individual loop operations.
	- **The first loop has n/2 operations**
	- The second loop has n^2 operations
	- **They are NOT nested loops.**
		- One loop executes AFTER the other completely finishes
	- So we simply ADD their operations
	- The total number of operations would be $n/2 + n^2$
	- In Big-O terms, we can express the number of operations as $O(n^2)$

- Example 2:
	- Determine the Big O running time of the following code fragment:

```
int func1(int n) {
      int i, j, x = 0;
      for (i = 1; i \le n; i++)for (j = 1; j <= n; j++)x++;
             }
      }
      return x;
}
```


Example 2:

- So look at what's going on in the code:
	- **We care about the total number of REPETITIVE** operations
	- **Ne have two loops**
		- **AND they are NESTED loops**
	- The outer loop runs n times
		- From $i = 1$ up through n
		- How many operations are performed at each iteration?
			- **Answer is coming...**
	- **The inner loop runs n times**
		- From $j = 1$ up through n
		- And only one operation (x++) is performed at each iteration

- Example 2:
	- So look at what's going on in the code:
		- **Let's look at a couple of iterations of the OUTER loop:**
			- When $i = 1$, what happens?
				- **The inner loop runs n times**
				- Resulting in n operations from the inner loop
			- Then, i gets incremented and it becomes equal to 2
			- When $i = 2$, what happens?
				- **Again, the inner loop runs n times**
				- Again resulting in n operations from the inner loop
		- **No. 19 Member of the following:**
			- **For EACH iteration of the OUTER loop,**
			- The INNER loop runs n times
				- Resulting in n operations

Example 2:

- So look at what's going on in the code:
	- **And how many times does the outer loop run?**
		- n times
	- So the outer loop runs n times
	- **And for each of those n times, the inner loop also runs** n times
		- **Resulting in n operations**
	- So we have n operations per iteration of OUTER loop
	- **And outer loop runs n times**
	- **Finally, we have n^{*}n as the number of operations**
	- We approximate the running time as $O(n^2)$

- Example 3:
	- Determine the Big O running time of the following code fragment:

```
int func3(int n) {
       int i, x = 0;
       for (i = 1; i <= n; i++) 
              x++;
       for (i = 1; i<=n; i++) 
              x++;
       return x;
}
```


Example 3:

- So look at what's going on in the code:
	- **We care about the total number of REPETITIVE** operations
	- **Ne have two loops**
		- They are NOT nested loops
	- The first loop runs n times
		- From $i = 1$ up through n
		- only one operation (x++) is performed at each iteration
	- **How many times does the second loop run?**
		- Notice that i is indeed reset to 1 at the beginning of the loop
		- Thus, the second loop runs n times, from $i = 1$ up through n
		- And only one operation (x++) is performed at each iteration

Example 3:

- So look at what's going on in the code:
	- **Again, the loops are NOT nested**
	- So they execute sequentially (one after the other)

Therefore:

- Our total runtime is on the order of n+n
- **Number 10 Number Which of course equals 2n**
- Now, in Big O notation
	- We approximate the running time as $O(n)$

- Example 4:
	- Determine the Big O running time of the following code fragment:

- Example 4:
	- So look at what's going on in the code:
		- We have one while loop
			- You can't just look at this loop and say it iterates n times or n/2 times
			- Rather, it continues to execute as long as n is greater than 0
			- The question is: **how many iterations will that be?**
		- **Number 19 Mile Loop**
			- **The last line of code divides the input, n, by 2**
			- **So n is halved at each iteration of the while loop**
		- If you remember, we said this ends up running in log n time
		- **Now let's look at how this works**

- Example 4:
	- So look at what's going on in the code:
		- **For the ease of the analysis, we make a new variable**
			- originalN:
				- originalN refers to the value originally stored in the input, n
				- So if n started at 100, originalN will be equal to 100
		- The first time through the loop
			- n gets set to originalN/2
				- If the original n was 100, after one iteration n would be 100/2
		- The second time through the loop
			- n gets set to originalN/4
		- The third time through the loop
			- n gets set to originalN/8

Notice:

After **three** iterations, n gets set to originalN/2**3**

- Example 4:
	- So look at what's going on in the code:
		- In general, after k iterations
			- n gets set to originalN/2k
		- The algorithm ends when originalN/ $2^k = 1$, approximately
		- We now solve for k
		- \blacksquare Why?
			- Because we want to find the **total # of iterations**
		- Multiplying both sides by 2^k , we get originalN = 2^k
		- **Now, using the definition of logs, we solve for k**
			- $k = log originalN$
		- So we approximate the running time as $O(log n)$

Brief Interlude: Human Stupidity

- Example 5:
	- Determine the Big O running time of the following code fragment:

```
int func5(int** array, int n) {
      int i = 0, j = 0;
      while (i < n) {
             while (j < n && array[i][j] == 1)
                     j++;
              i++;
       }
      return j;
}
```
Example 5:

- So look at what's going on in the code:
	- **At first glance, we see two NESTED loops**
	- This can often indicate an $O(n^2)$ algorithm
		- But we need to look closer to confirm
	- Focus on what's going on with i and j

```
int func5(int** array, int n) {
      int i = 0, j = 0;
      while (i < n) {
             while (j < n && array[i][j] == 1)
                    j++;
             i++;
       }
```
- Example 5:
	- So look at what's going on in the code:
		- Focus on what's going on with i and j
			- i and j clearly increase (from the $j++$ and $j++$)
			- **BUT, they never decrease**
			- **AND, neither ever gets reset to 0**

```
int func5(int** array, int n) {
      int i = 0, j = 0;
      while (i < n) {
             while (j < n && array[i][j] == 1)
                    j++;
             i++;
       }
```


Example 5:

- So look at what's going on in the code:
	- **And the OUTER while loop ends once i gets to n**
	- So, what does this mean?
		- The statement i++ can never run more than n times
		- And the statement *j*++ can never run more than n times

```
int func5(int** array, int n) {
      int i = 0, j = 0;
      while (i < n) {
             while (j < n && array[i][j] == 1)
                    j++;
             i++;
       }
```


Example 5:

- So look at what's going on in the code:
	- **The MOST number of times these two statements can** run (combined) is 2n times
	- So we approximate the running time as $O(n)$

int func5(int array, int n) { int i = 0, j = 0; while (i < n) { while (j < n && array[i][j] == 1) j++; i++; }**

Example 6:

Determine the Big O running time of the following code fragment:

■ What's the one big difference here???

```
int func6(int** array, int n) {
      int i = 0, j;
      while (i < n) {
             j = 0;
              while (j < n && array[i][j] == 1)
                     j++;
              i++;
       }
      return j;
}
```


- Example 6:
	- So look at what's going on in the code:
		- The difference is that we RESET j to 0 a the beginning of the OUTER while loop

```
int func6(int** array, int n) {
      int i = 0, j;
      while (i < n) {
             j = 0;
              while (j < n && array[i][j] == 1)
                     j++;
              i++;
       }
      return j;
}
```


Example 6:

- So look at what's going on in the code:
	- The difference is that we RESET j to 0 a the beginning of the OUTER while loop
	- **How does that change things?**
		- Now j can iterate from 0 to n for EACH iteration of the OUTER while loop
			- **For each value of i**
		- \blacksquare This is similar to the 2nd example shown
	- So we approximate the running time as $O(n^2)$

- Example 7:
	- Determine the Big O running time of the following code fragment:

```
int func7(int A[], int sizeA, int B[], int sizeB) {
      int i, j;
      for (i = 0; i < sizeA; i++)
             for (j = 0; j < sizeB; j++)
                    if (A[i] == B[j])
                           return 1;
      return 0;
}
```


Example 7:

- So look at what's going on in the code:
	- **First notice that the runtime here is NOT in terms of n**
	- \blacksquare It will be in terms of sizeA and sizeB
	- **And this is also just like Example 2**
	- **The outer loop runs sizeA times**
	- **For EACH of those times,**
		- The inner loop runs sizeB times
	- So this algorithm runs sizeA*sizeB times
	- We approximate the running time as O(sizeA*sizeB)

- Example 8:
	- Determine the Big O running time of the following code fragment:

```
int func8(int A[], int sizeA, int B[], int sizeB) {
      int i, j;
      for (i = 0; i < sizeA; i++) {
             if (binSearch(B, sizeB, A[i]))
                    return 1;
       }
      return 0;
}
```


Example 8:

- So look at what's going on in the code:
	- Note: we see that we are calling the function binSearch
	- **As discussed previously, a single binary search runs in** O(log n) time
		- where n represents the number of items within which you are searching
- **Examining the for loop:**
	- The for loop will execute sizeA times
	- **For EACH iteration of this loop**
		- a binary search will be run
	- We approximate the running time as O(sizeA*log(sizeB))

WASN'T THAT SWEET!

Daily Demotivator

NO MATTER HOW WRONG YOURS MAY BE.

Computer Science Department University of Central Florida

COP 3502 – Computer Science I