

COP 3502 10/18/21

Announcements

- ① ^{FRIDAY} Recitation starts after 2 pm is cancelled.
RP program still exists. You may elect to do it. You definitely can do it during the scheduled recitation time.
- ② ^D TURN IN STUDY GROUPS THIS SUNDAY. If you're in a TA one, they'll give me the attendance, etc.

~~MERGE~~ SORT MERGE

Works because of Merge

Input: 2 sorted lists

Output: a merged sorted list with each item from either input list

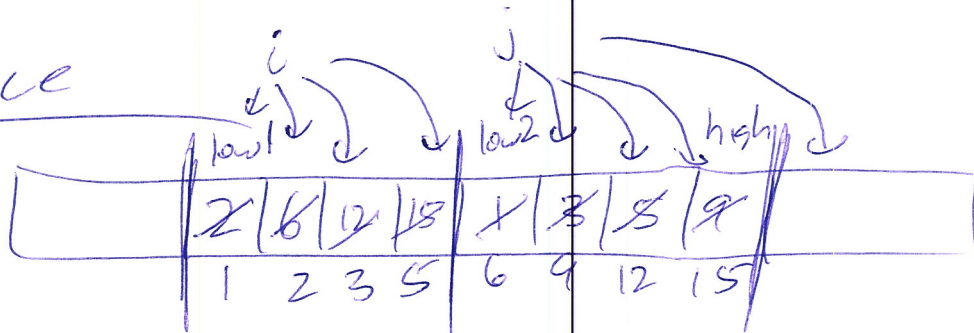
n List 1: 2, 6, 8, 9, 15, 17 (6 items)
m List 2: 3, 4, 5, 11, 20, 22, 45, 57 (8 items)

Output: 2, 3, 4, 5, 6, 8, 9, 11, 15, 17, 20, 22, 45, 57

basically iterate through both lists, always take the smallest value + update that index.

Runtime: $O(n+m)$

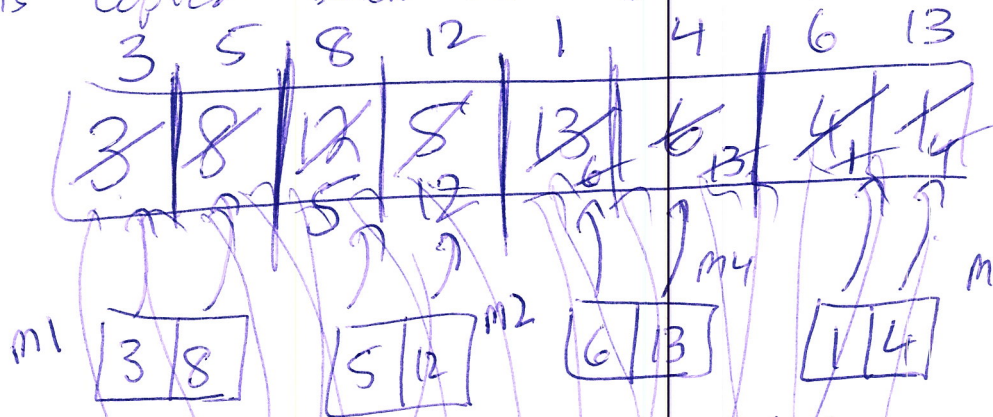
Practice



temp

1	2	3	5	6	9	12	15
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2 arrays are side by side in 1 array and indicated by starting/ending indexes + result is copied back into the main array.



m1

3	8
---	---

m2

5	12
---	----

m4

6	13
---	----

m5

1	4
---	---

m3

3	5	8	12
---	---	---	----

1	4	6	13
---	---	---	----

m7

1	3	4	5	6	8	12	13
---	---	---	---	---	---	----	----

~~ms(7,7)~~
~~ms(6,6)~~
~~ms(6,7)~~
~~ms(5,5)~~
~~ms(4,4)~~
~~ms(4,5)~~
~~ms(4,7)~~
ms(0,7)

~~ms(3,3)~~
~~ms(2,2)~~
ms(2,3)
~~ms(1,1)~~
~~ms(0,0)~~
~~ms(0,1)~~
~~ms(0,3)~~
ms(0,7)

Merge Sort

Merge

Input: 2 sorted list

Output: 1 sorted list w/ each item
from the 2 old lists.

LIST 1: ~~3~~ ~~6~~ ~~9~~ ↓ 11, 15, 45, 47, 53, 56

LIST 2: 2, 5, 7, 8, ~~12~~ ~~13~~ ~~22~~ ~~25~~ ~~27~~ ↑

OUTPUT: 2, 3, 5, 6, 7, 8, 9, 11, ...

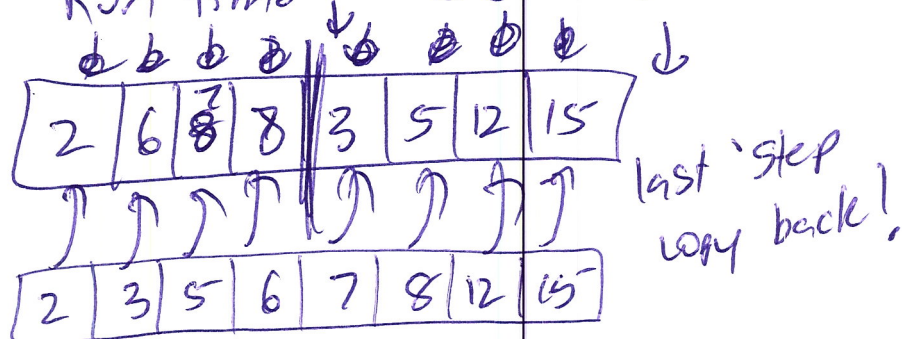
ALG: start 2 ptrs (integer indexes)
into both lists at 0, repeatedly copy
smaller value into the next slot in the
out put array. (Once you run out of a
list just copy the other list over.)

- Array out of Bounds
- Test w/ array sizes 1, 2, etc.

n = Size of list 1

m = Size of list 2

Merge Run time = $O(n+m)$



How can we use this tool to sort?



① MS(Left) ② MS(Right)

③  Merge back

Void MergeSort(int* array, int low, int high) {

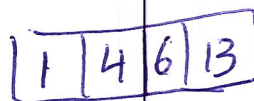
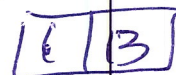
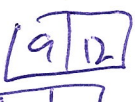
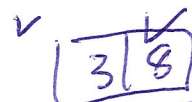
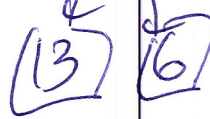
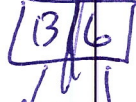
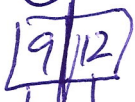
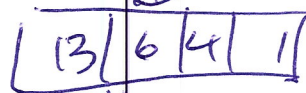
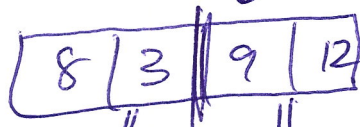
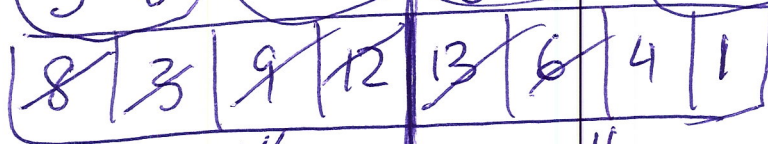
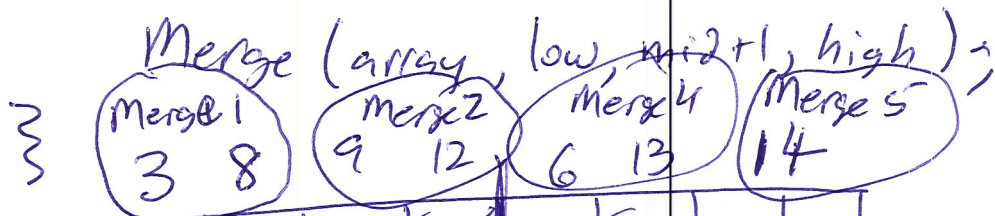
if (low >= high) return;

int mid = (low + high) / 2;

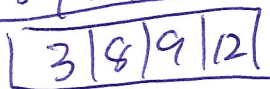
MergeSort(array, low, mid);

MergeSort(array, mid+1, high);

Merge(array, low, mid+1, high);



Merge 3

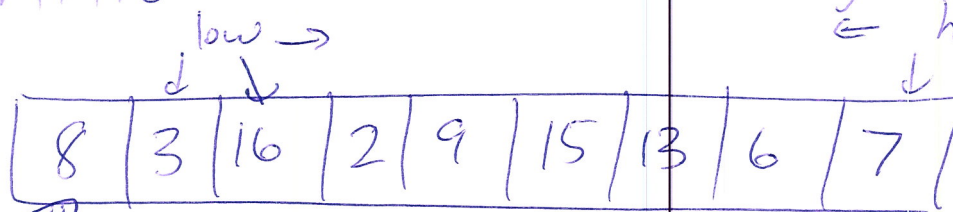


Merge 6

~~MS(5,5)~~
~~MS(4,4)~~
~~MS(4,3)~~
~~MS(4,2)~~
~~MS(0,7)~~

~~MS(3,3)~~
~~MS(2,2)~~
~~MS(2,3)~~
~~MS(1,1)~~
~~MS(0,0)~~
~~MS(0,1)~~
~~MS(0,3)~~
~~MS(0,7)~~

Partition of an array



Partition
Element

Everything $<$ PartElem $\Rightarrow$ left

Everything $>$ PartElem $\Rightarrow$ right

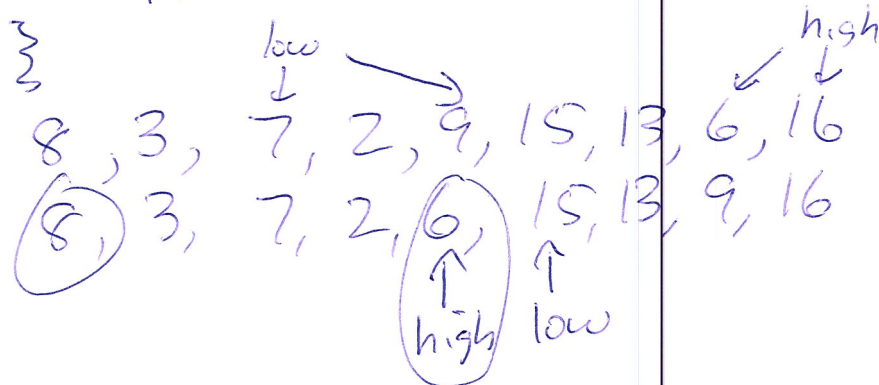
Goal: after we're done, everything left PartElem is less than it, everything right of PartElem is greater than it.

while (low $\neq$ high) {

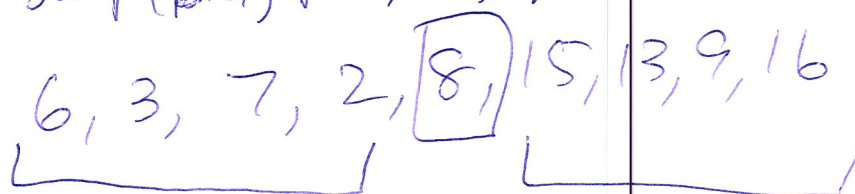
while (low $<$ end && $a[\text{low}] < a[\text{part}]$) low++;

while (high $>$ part && $a[\text{high}] \geq a[\text{part}]$) high--;

if (low $\neq$ high) swap(a, low, high);



swap(a, part, high)



sort

sort ✓