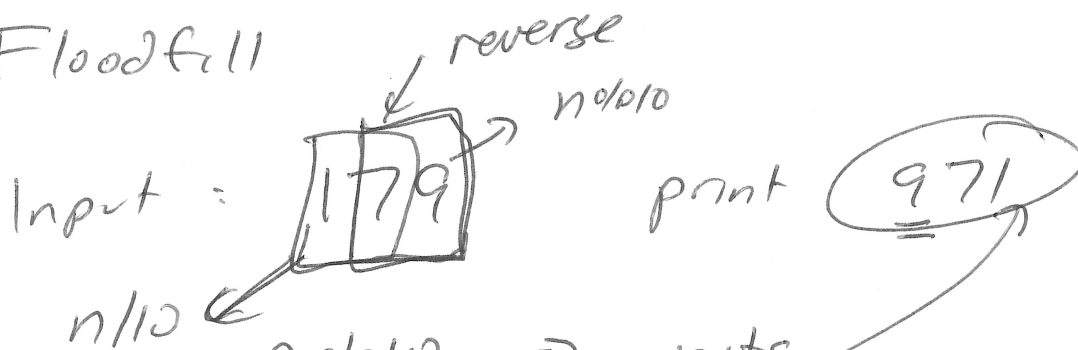
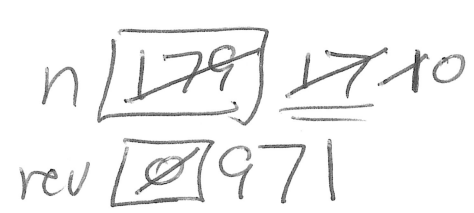


# Recursion

- Reversing Number (printing)
- ~~Base Conversion~~
- Counting occurrences of a letter in string
- Fast Mod Expo
- Floodfill

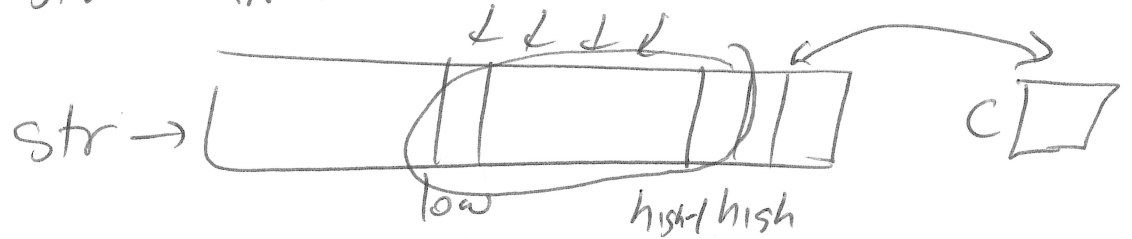


```
n/10 => units  
printf("%d", n/10)  
rec(n/10);
```



```
int rev = 0;  
while (n > 0) {  
    rev = 10 * rev + n/10;  
    n /= 10;  
}
```

Count # times char c appears in  
string str from index low to index high



return `count(str, low, high-1, c) + (str[high] == c);`

## Fast Mod Expo

$b^e \text{ \% mod}$

Run time  
 $O(\log e)$

## Slow Mod Expo

`res = 1`

for (`i = 0; i < exp; i++`)

`res = (res * base) \% mod;`

return `res;`

$$b^{1000000} = b^{500000} \times b^{500000}$$

Divide  
Conquer

if (`exp \% 2 == 0`) {  
`tmp = fastmodexpo(base, exp/2, mod);`  
 return `(tmp * tmp) \% mod;`  
 }

1000000 → 500,000 → 250,000 → 125,000 → 62500  
 → 31250 → 15625 → 15624 → 7812

$$b^e = b^{e-1} \times b$$

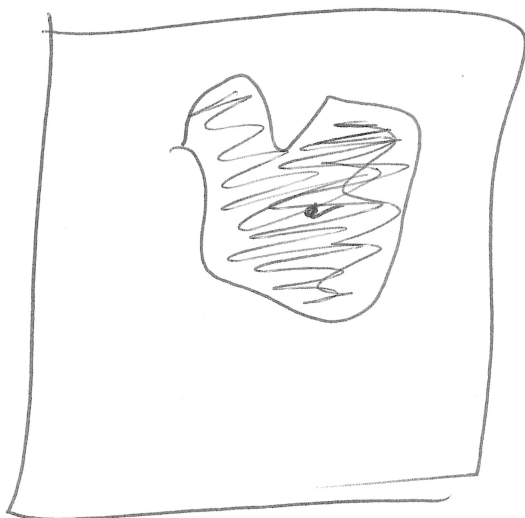
2 steps divide exp by 2

$$\frac{\text{exp}}{2^k} = 1 \quad \text{exp} = 2^k$$

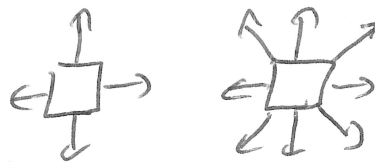
$$k = \log_2 \text{exp}$$

$$\# \text{ rec calls} \leq 2 \cdot \log_2 \text{exp}$$

## Floodfill



□ Print Bucket



floodfill ( int x, int y, int\*\* grid, int\*\* used ) {

if (! inbounds(x,y)) return;  
 if ( used[x][y] ) return;  
 if ( is boundary(x,y) ) return;

grid[x][y] = fillColor;

used[x][y] = 1;

for each neighbor of (x,y)

floodfill(x', y', grid, used);

}

const int DX[4] = { -1, 0, 0, 1 };

const int DY[4] = { 0, 1, 1, 0 };

for (int i = 0; i < 4; i++)

int nx = x + DX[i];

int ny = y + DY[i];

floodfill(nx, ny, ...);

}

x[3]

y[5]

(2, 5)

(3, 4)

(3, 6)

(4, 5)