

CWP 3502 10/18/23

Merge Sort $\rightarrow O(n \lg n)$ best, avg, worst

Merge Algorithm

Input: 2 sorted lists

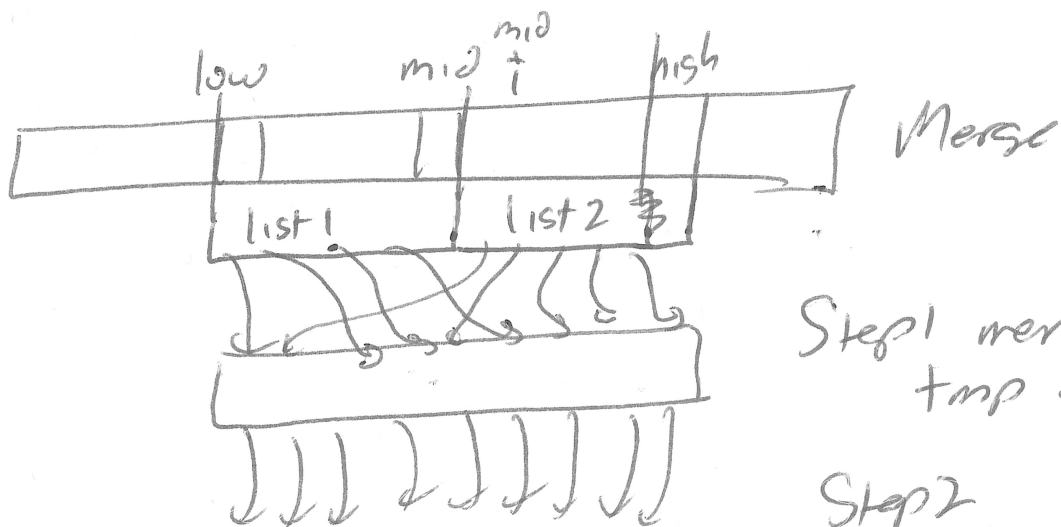
Output: a single sorted list with all items from the 2 input lists

list 1: $i=0$
1, 6, 8, 10, 15 n

list 2: $j=0$
3, 4, 7, 11 m

$O(n+m)$

list 3 = $k=0$
1, 3, 4, 6, 7, 8, 10, 15

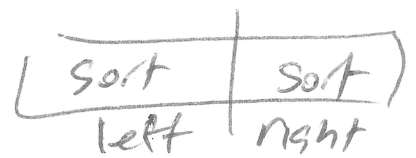


Step 1 merge into temp array

Step 2
Copy back into orig array

Step 3 free temp

Merge Sort



```
void sort (int* arr, int n) {
```

```
    mergesort (arr, 0, n-1);
```

```
void mergesort (int* arr, int low, int high) {
```

```
    if (low >= high) return;
```

```
    int mid = (low+high)/2;
```

```
    mergesort (arr, low, mid);
```

```
    mergesort (arr, mid+1, high);
```

```
    merge (arr, low, mid, high);
```

$$T(n) = T\left(\frac{n}{2}\right) + T\left(\frac{n}{2}\right) + O(n)$$

$$T(n) = 2T\left(\frac{n}{2}\right) + O(n)$$

Master's Thm $A=2, B=2, k=1 \Rightarrow O(n \log n)$

~~MS(0,0) MS(1,1)~~

~~MS(0,1) MS(2,3)~~

~~MS(0,3)~~

MS(0,7)

~~M(4,5) M(6,7)~~

~~M(4,7)~~

M(0,7)