

COP3502 4/4/22

(1) Video - Trees

(2) Δ Syllabus

(3) Quiz 4 - Friday

(4) Heaps - PG data structure

1st hand way to learn these ideas

- closer to something real world
- rules "messy"
- ~~then~~ sizeable example where you have to be very careful with dynamically allocated memory.

Binary Heap

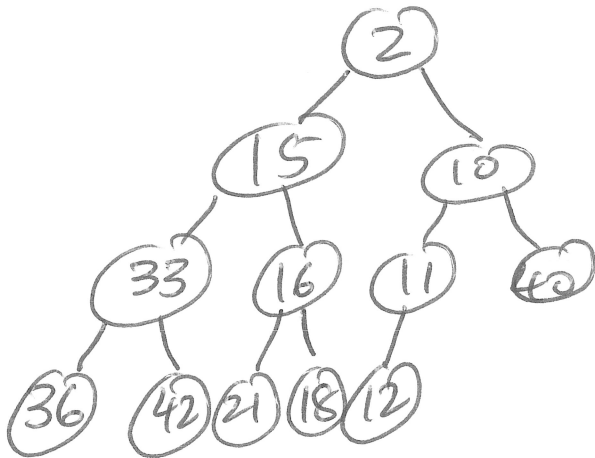
algⁿ)

- Insert items
- Delete Min

} 2 operations support.

run times similar to ^a Balanced BST.
Maybe a little simpler implementation

Binary Heap Drawing



for any node, everything
in its subtree is
greater than it!
→ heap node property.

added nodes
top to bottom
left to right

→ complete
binary
tree

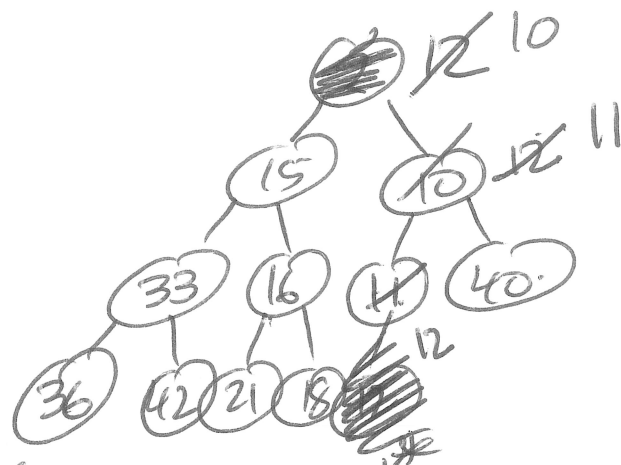
In order to be a
Valid binary heap,
we need to be a
(1) complete binary tree
(2) obey heap node property.

To store in code

	2	15	10	33	16	11	40	36	42	21	18	12
0	1	2	3	4	5	6	7	8	9	10	11	12

array - for node at index i ,
left child index $2i$
right child index $2i+1$
its parent is at index $i/2$ (int div)

- ① Delete Min
- ② Insert



Delete Min

- ① CEO takes off! (remove 1st slot)
- ② Mail boy realizes CEO gone. (copy last item into 1st slot)
- ③ VPs (child nodes) realize they should be in that spot. The lower number swaps w/ mailboy. Continue until mailboy finds a valid spot in the hierarchy

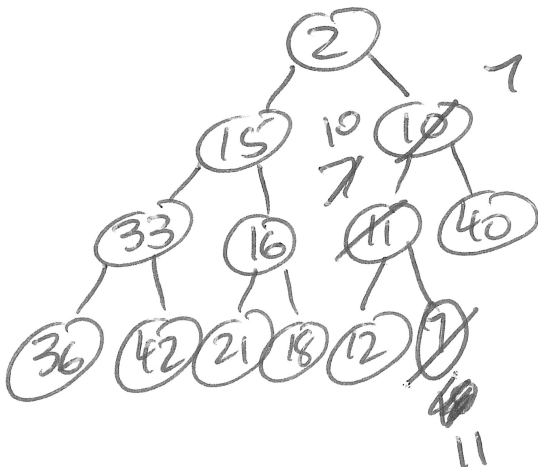
Percolate Down

PERCOLATE

Run time: $n = 2^{h+1} - 1$ nodes
or at min $n = 2^h$ nodes

$$h \leq \log_2 n$$

Insert



Insert 7

- ① Add item in next valid location
- ② Percolate UP
 - node challenges parent
 - swap if out of order

heap example picture

list →

n [4]

