

COP 3502 4/13/22

Bitwise Operators

In computer all #s stored in base 2 (binary)

$$13 = \underbrace{0 \dots 0}_{28 \text{ 0's}} \underbrace{1101}_{4 \text{ bits}}$$

each int is stored in 32 bits

regular int is signed $\Rightarrow$ MSB (most sig bit) is worth -2^{31} not 2^{31} . (2's complement)

$$\underbrace{100 \dots 0}_{31 \text{ 0's}} = -2^{31}$$

$$\underbrace{011 \dots 1}_{31 \text{ 1's}} = 2^{31} - 1$$

range int

$$[-2^{31}, 2^{31} - 1]$$

In general, if we used b bits in 2's comp range $[-2^{b-1}, 2^{b-1} - 1]$.

Regular boolean $\&\&$, $\|\|$, $!$
operators and or not

WORK on individual booleans (0 or 1)

An int is really an array of "booleans"

$$13 = \begin{array}{c} 31 \qquad \qquad \qquad 3 \quad 2 \quad 1 \quad 0 \\ \boxed{0 \mid 0 \mid 0 \mid 0 \mid \dots \mid \dots \mid 1 \mid 1 \mid 0 \mid 1} \end{array}$$

array in reverse! 0 = False, 1 = True

bitwise ops

$$\& \quad (\text{and}) \quad \begin{array}{r} 13 \\ 97 \end{array} = \begin{array}{r} 00001101 \\ 01100001 \\ \hline 00000001 = 1 \end{array}$$

$$| \quad (\text{or}) \quad \begin{array}{r} 13 \\ 97 \end{array} = \begin{array}{r} 00001101 \\ 01100001 \\ \hline 01101101 = 109 \end{array}$$

$$\wedge \quad (\text{xor}) \quad \begin{array}{r} 13 \\ 97 \end{array} = \begin{array}{r} 00001101 \\ 01100001 \\ \hline 01101100 = 108 \end{array}$$

$$\sim \quad (\text{not}) \quad \sim 13 \Rightarrow \text{all 1's} \Rightarrow 0$$

$$0's \Rightarrow 1$$

In practice,

$$\sim n = -(n+1) \quad \sim 13 = -14$$

when $n > 0$

flips all bits

$>>$ (right shift) $97 >> 3$
 move over the binary representation of
 97 by 3 places to the right
 (chop off the last 3 bits)
 dividing int by 2^3 .

$$97 \quad 1100001$$

$$97 >> 3 = 1100 = 12$$

$<<$ (left shift) $13 << 2$
 move over binary of 13 by 2 places left.

$\rightarrow \text{mult } 2^2$

$$13 = 1101, 13222 = 110100$$

Examples of USE

① Counting differences OR similarities

$$\begin{array}{cccccccc}
 & T & T & F & T & F & T & F \\
 X = & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & \text{(my quiz ans)} \\
 \wedge Y = & 1 & 0 & 1 & 1 & 1 & 1 & 0 & 1 & \text{(correct)}
 \end{array}$$

$$X \wedge Y = 01101011 \quad (\# \text{ bits on are differences})$$

5 bits on means 5 slots are different

$$\text{my score} = 8 - 5$$

$$\text{got wrong} = 5$$

② Union or intersection of 2 sets

$$\begin{array}{lcl}
 \text{cur} & = & 000000010101101 \\
 1 \text{ pack} & = & 0110000100000000
 \end{array}$$

$$\text{cur} \vee \text{pack} = 011000010101101$$

bits on = # unique cards in collection

Intersection would be 8

(only items belonging to both sets will be highlighted)