

1. (10 points) [UseModels] Write, in Oz, a tail-recursive function:

```
Duplicate: <fun {$ <T> <Int>}: <List <T>> >
```

that takes a value, V, of some type T, and an integer N, and returns a list of length N in which each element is V. Your code should assume that N is non-negative.

Your solution must have iterative behavior, and must be written using tail recursion. Don't use any higher-order functions, and don't use the Oz **for** loop syntax in your solution! (You are supposed to know what these directions mean.)

The following are examples.

```
% $Id: DuplicateTest.oz,v 1.1 2012/03/18 01:58:38 leavens Exp leavens $
\insert 'Duplicate.oz'
\insert 'TestingNoStop.oz'
{StartTesting 'DuplicateTest.oz $Revision: 1.1 $'}
{Test {Duplicate x 0} '==' nil}
{Test {Duplicate b 3} '==' b|b|b|nil}
{Test {Duplicate a 7} '==' a|a|a|a|a|a|a|nil}
{Test {Duplicate 5 10} '==' [5 5 5 5 5 5 5 5 5]}
{Test {Duplicate nil 2} '==' [nil nil]}
{Test {Duplicate easy 1} '==' [easy]}
{Test {Duplicate easy 5} '==' [easy easy easy easy easy]}
{Test {Duplicate [o k] 3} '==' [[o k] [o k] [o k]]}
{DoneTesting}
```

2. (10 points) [UseModels] Without using a **for**-loop, **FoldR**, or **Map**, write in Oz the function

```
Scale: <fun {$ <List Int> <Int>}: <List Int>>
```

that takes a list of integers, **LoI**, and an integer, **Factor**, and returns a list integers in which each element is the result of multiplying **Factor** by the corresponding element in the original list. The following are examples.

```
% $Id: ScaleTest.oz,v 1.1 2012/03/18 01:58:38 leavens Exp leavens $
\insert 'Scale.oz'
\insert 'TestingNoStop.oz'
{StartTesting 'ScaleTest.oz $Revision: 1.1 $'}
{Test {Scale nil 100} '==' nil}
{Test {Scale 5|nil 100} '==' 500|nil}
{Test {Scale 6|5|nil 100} '==' 600|500|nil}
{Test {Scale [3 4 3 2] 10} '==' [30 40 30 20]}
{Test {Scale [3 ~4 7 ~2] 0} '==' [0 0 0 0]}
{Test {Scale [7 9 2 8 7 2 1 0 ~4 60] ~18} '==' [~126 ~162 ~36 ~144 ~126 ~36 ~18 0 72 ~1080]}
{DoneTesting}
```

3. (10 points) [UseModels] Using Oz's built-in **FoldR** function, write the function

```
Scale: <fun {$ <List <Int>> <Int>}: <List <Int>>>
```

from the previous problem.

Your solution must use Oz's built-in **FoldR** function (but you can also write additional helping functions if you wish)! So you must fill in your answer by completing the code outline below.

declare

```
fun {Scale LoI Factor}
  {FoldR
```

```
  }
```

```
end
```

4. (10 points) [Concepts] [UseModels] Write a curried version of the function Compose, shown below.

```
declare
fun {Compose F G X}
  {F {G X}}
end
```

The function you are to write should be called CurriedCompose. That is, write

```
CurriedCompose: <fun {$ <fun {$ <S>}: <U>>}:
  <fun {$ <fun {$ <T>}: <S>>}:
    <fun {$ <T>}: <U>>>>
```

such that, CurriedCompose takes a function, F, and returns a function that takes as an argument a function, G, and which returns a function that itself takes an argument, X, and returns the value of {F {G X}}.

The following are examples.

```
% $Id: CurriedComposeTest.oz,v 1.1 2012/03/18 01:58:38 leavens Exp leavens $
\insert 'CurriedCompose.oz'
\insert 'TestingNoStop.oz'
{StartTesting 'CurriedComposeTest.oz $Revision: 1.1 $'}
{Test {{{CurriedCompose Not} IsList} 3} '==' {Not {IsList 3}}
{Test {{{CurriedCompose IsInt} Length} nil} '==' {IsInt {Length nil}}
{Test {{{CurriedCompose IsInt} fun {$ X} X+3 end} 7} '==' {IsInt 10}}
{Test {{{CurriedCompose fun {$ Y} Y*5 end} fun {$ X} X+3 end} 7} '==' 50}
{Test {{{CurriedCompose fun {$ Y} Y*5 end} fun {$ X} X+10 end} 3} '==' 65}
{DoneTesting}
```

Please write your answer below.

5. (10 points) [UseModels] In Oz, write a function,

`ReplaceIn: <fun {$ <List <List <T>>> <T> <T>}: <List <List <T>>>>` which takes a list of lists of elements of some type T, LL, and two elements of type T, Old and New, and returns a list of lists that is just like LL, except that all occurrences of Old in the inner lists are replace by New. The following are examples.

```
% $Id: ReplaceInTest.oz,v 1.2 2012/03/18 01:58:38 leavens Exp leavens $
\insert 'ReplaceIn.oz'
\insert 'TestingNoStop.oz'
{StartTesting 'ReplaceInTest.oz $Revision: 1.2 $'}
{Test {ReplaceIn nil old new} '==' nil}
{Test {ReplaceIn [[foo bar old stuff]] old new} '==' [[foo bar new stuff]]}
{Test {ReplaceIn [[old old] nil [foo bar old stuff]] old new} '==' [[new new] nil [foo bar new stuff]]}
{Test {ReplaceIn [[7 6 5] [3 2] [9 3 1 2] [7 8]] 2 22} '==' [[7 6 5] [3 22] [9 3 1 22] [7 8]]}
{Test {ReplaceIn [{"a" "bad" "" "scene"} {"was" "" "troubling"}] "" "fng"}
'==' [{"a" "bad" "fng" "scene"} {"was" "fng" "troubling"}]}
{DoneTesting}
```

6. (15 points) [UseModels] Consider the following grammar

```

<Route> ::= route(<List <Place>>)
<Place> ::= place(where: <Atom> features: <List <Atom>>)

```

In Oz, write a function, `AddFeature: <fun {$ <Route> <Atom> <Atom>}: <Route>>` which takes a `<Route>`, `R`, and two atoms `Where` and `What`, and returns a `<Route>` that is just like `R`, except that in each `<Place>` whose `where` field is (`==` to) `Where`, `What` is added to the front of the list in that `Place`'s `features` field. Here are examples:

```

\insert 'AddFeature.oz'
\insert 'TestingNoStop.oz'
{StartTesting 'AddFeatureTest.oz $Revision: 1.1 $'}
{Test {AddFeature route(nil) dennys pancakes} '==' route(nil)}
{Test {AddFeature route(place(where: dennys features: cokes|icecream|nil)|nil) dennys pancakes}
  '==' route(place(where: dennys features: pancakes|cokes|icecream|nil)|nil)}
{Test {AddFeature route([place(where: iceland features: [cold]) place(where: iceland features: [ice]))
  iceland herring}
  '==' route([place(where: iceland features: [herring cold]) place(where: iceland features: [herring ice]))}
{Test {AddFeature route([place(where: atlanta features: [grits baseball]) place(where: paris features: [wine])
  place(where: berlin features: [donuts]) place(where: berlin features: [museums])
  place(where: paris features: [art]) place(where: atlanta features: [basketball]))]
  paris moonlight}
  '==' route([place(where: atlanta features: [grits baseball]) place(where: paris features: [moonlight wine])
  place(where: berlin features: [donuts]) place(where: berlin features: [museums])
  place(where: paris features: [moonlight art]) place(where: atlanta features: [basketball]))]}
{DoneTesting}

```

7. (15 points) [UseModels] This problem uses the same grammar for $\langle \text{Route} \rangle$ as the previous problem.

```

 $\langle \text{Route} \rangle ::= \text{route}(\langle \text{List} \langle \text{Place} \rangle \rangle)$ 
 $\langle \text{Place} \rangle ::= \text{place}(\text{where: } \langle \text{Atom} \rangle \text{ features: } \langle \text{List} \langle \text{Atom} \rangle \rangle)$ 

```

In Oz, write the function `PlacesMap`: `<fun {$ <Route> <fun {$ <Place>}: <Place>>}: <Route>>`, which takes a route, `R`, and a function `PF`, (where `PF` takes a $\langle \text{Place} \rangle$ and returns a $\langle \text{Place} \rangle$), and returns a route that has the same shape as `R`, except that each $\langle \text{Place} \rangle$, `P`, in the route is replaced by the result of applying `PF` to `P`. Here are examples:

```

\insert 'PlacesMap.oz'
\insert 'TestingNoStop.oz'
{StartTesting 'PlacesMapTest.oz $Revision: 1.1 $'}
{Test {PlacesMap route(nil) fun {$ P} place(where: nowhere features: nil) end}
  '==' route(nil)}
{Test {PlacesMap route([place(where: paris features: [wine cheese]) place(where: delhi features: [chai curry])])
  fun {$ P} place(where: nowhere features: nil) end}
  '==' route([place(where: nowhere features: nil) place(where: nowhere features: nil)])}
{Test {PlacesMap route([place(where: orlando features: [disney universal])
  place(where: paris features: [wine cheese])
  place(where: delhi features: [chai curry])])
  fun {$ P} case P of
    place(where: paris features: _) then place(where: paris features: [degalle roissy])
    [] place(where: delhi features: _) then place(where: delhi features: [gandhi])
    else P
  end
  end}
  '==' route([place(where: orlando features: [disney universal])
  place(where: paris features: [degalle roissy])
  place(where: delhi features: [gandhi])])}
{DoneTesting}

```

8. (20 points) [UseModels] This problem works with the type $\langle \text{Order} \rangle$, as defined by the following grammar (where a $\langle \text{String} \rangle$ is, as usual, a $\langle \text{List Char} \rangle$).

```

<Order> ::= order(<List Item>)
<Item> ::= drink(what: <Atom> price: <Int>)
         | food(what: <Atom> price: <Int>)
         | combo(<List Item>)

```

In Oz, write a function

```
OrderCost: <fun {$ <Order>}: <Int>>
```

that takes an $\langle \text{Order} \rangle$, `Ord`, and return the sum of the cost of the items in the `Order`'s list. The *cost* of an $\langle \text{Item} \rangle$ is the $\langle \text{Int} \rangle$ in the price field in a `drink` or `food` record, and the sum of the costs of the items in the list of items in a `combo` record.

```

\insert 'OrderCost.oz'
\insert 'TestingNoStop.oz'

{StartTesting 'OrderCostTest.oz $Revision: 1.1 $'}
{Test {OrderCost order(nil)} '==' 0}
{Test {OrderCost order([drink(what: beer price: 3)])} '==' 3}
{Test {OrderCost order([drink(what: beer price: 3)
                        drink(what: coke price: 2)])} '==' 5}
{Test {OrderCost order([drink(what: pepsi price: 2)
                        food(what: burger price: 8)])} '==' 10}
{Test {OrderCost order([drink(what: water price: 2)
                        drink(what: tea price: 2)
                        drink(what: sprite price: 3)
                        food(what: coupon price: ~3)
                        food(what: salad price: 6)
                        food(what: steak price: 15)
                        combo([food(what: hsalad price: 3)
                              food(what: chop price: 10)])])}
      '==' 38}
{Test {OrderCost order([combo([combo([drink(what: water price: 0)
                                      drink(what: coffee price: 1)])
                                combo([food(what: blt price: 5)
                                      food(what: cuban price: 8)
                                      food(what: chips price: 0)])])])}
      '==' 14}
{Test {OrderCost order([drink(what: water price: 2)
                        combo([drink(what: wine75 price: 15)
                                food(what: foisgras price: 30)
                                drink(what: wine79 price: 14)
                                food(what: duck price: 35)
                                combo([food(what: wine24 price: 12)
                                      food(what: chocolatemousse price: 10)])])
                        drink(what: coffee price: 3)])}
      '==' 121}
{DoneTesting}

```

There is room for your answer on the next page.

Please put your answer to the OrderCost problem below.