

1. [Concepts] This is a question about free and bound identifiers in Erlang code. As in the homework, both variable names and function names are considered to be identifiers.

Consider the following Erlang expression.

```
concat(map(fun(Y) -> F(X,Y) end, (fun(Q,R) -> Q end)(LS,empty)))
```

- (a) (10 points) In set brackets ({ and }), list the complete set of all identifiers that occur free in the above expression.

- (b) (4 points) In set brackets ({ and }), list the complete set of all identifiers that occur bound in the above expression.

2. (6 points) [Concepts] In Erlang, will there necessarily be a type error if one puts different types of elements in a single list, like the following?

```
[3, true, foo, $c, [1,2], [ok,sure], 5.2, self()]
```

Answer “yes” or “no” and give a brief justification.

3. (10 points) [UseModels] In Erlang, write a function `sumsquares/1`, which has the following type specification:

```
-spec sumsquares(LON :: [number()]) -> number().
```

This function takes a list of numbers, `LON`, and returns the sum of the squares of the numbers in `LON`. The following are tests using the homework's testing module.

```
-module(sumsquares_tests).
-export([main/0]).
-import(sumsquares,[sumsquares/1]).
-import(testing,[dotests/2,eqTest/3]).
main() -> compile:file(sumsquares),
        dotests("sumsquares_tests $Revision: 1.1 $", tests()).
tests() ->
    [eqTest(sumsquares([]), "=", 0),
     eqTest(sumsquares([3]), "=", 9),
     eqTest(sumsquares([4,3]), "=", 25),
     eqTest(sumsquares([1,2,4,3]), "=", 30),
     eqTest(sumsquares([1,10,500]), "=", 250101),
     % note that lists:seq(1,100) == [1,2,3,4,...,98,99,100]
     eqTest(sumsquares(lists:seq(1,100)), "=", 338350),
     eqTest(sumsquares([30|lists:seq(1,100)]), "=", 339250),
     eqTest(sumsquares(lists:seq(7,74321)), "=", 136842860543870) ].
```

4. (10 points) [UseModels] In Erlang, write a stateless server in a module named `average`. You should write a function `start/0` that returns the process id of a server. This server responds to messages of the form `{Pid, {average, LON}}`, where `Pid` is the sender's process id, and `LON` is a non-empty list of numbers. When the server receives such a message, it responds by sending a message of the form `{Self, {average_is, Res}}` to `Pid`, where `Self` is the server's process id, and `Res` is the average (arithmetic mean) of the numbers in `LON`. In your solution you can use the arithmetic operator `/` for division and the library function `lists:sum/1`, which returns the sum of a list of numbers. The following are tests.

```
-module(average_tests).
-export([main/0]).
-import(average,[start/0]).
-import(testing,[dotests/2,eqTest/3]).
-import(floattesting,[withinTest/3]). % withinTest checks for approximate equality
main() -> dotests("average_tests $Revision: 1.1 $", tests()).
tests() ->
  AS = start(),
  [withinTest(compute_average(AS, [1]),"~=",1.0),
   withinTest(compute_average(AS, [5,6,7]),"~=",6.0),
   withinTest(compute_average(AS, [100,5,6,7]),"~=",29.5),
   withinTest(compute_average(AS, [1.0,10.0,20.0,30.0,40.0]),"~=",20.2),
   withinTest(compute_average(AS, [3.14,9.86,21.5,32.7,88.514]),"~=",31.1428),
   withinTest(compute_average(AS, [100.0,100.1,100.2]),"~=",100.1) ].
%% helper for testing, NOT for you to implement.
-spec compute_average(AS::pid(), LON::[number()]) -> number().
compute_average(AS, LON) ->
  AS ! {self(), {average, LON}},
  receive {AS, {average_is, Res}} -> Res end.
```

5. (20 points) [UseModels] In an Erlang module named `catalogserver`, write a function `start/0`, which creates a catalog server and returns its process id. A server created by `catalogserver:start()` keeps track of a mapping from keys to values. The keys and values are both Erlang values (of any type). The server responds to two types of messages:

- `{Pid, {associate, Key, Value}}`, where `Pid` is the sender's process id, and `Key` and `Value` are both Erlang values. This message causes the server to remember that `Key` maps to `Value` (and forget any previous such association for `Key`). The server responds by sending to `Pid` a message of the form `{SPid, ok}`, where `SPid` is the server's process id.
- `{Pid, {lookup, Key}}`, where `Pid` is the sender's process id. The server responds by sending a message to `Pid` of the form `{SPid, {value_is, Value}}`, where `Value` is the value that the server is remembering as the value that `Key` maps to, and `undefined` if the server is not currently remembering a value that `Key` maps to. Again, `SPid` is the server's own process id.

The following are tests. There is space for your answer on the next page.

```
-module(catalogserver_tests).
-import(catalogserver,[start/0]).
-import(testing,[dotests/2,eqTest/3]).
-export([main/0, associate/3, lookup/2]).
main() -> dotests("catalogserver_tests $Revision: 1.3 $", tests()).
tests() -> compile:file(catalogserver),
  CS = start(), C2 = start(), % make 2 catalog servers
  [eqTest(lookup(CS, take),"=",undefined),
   eqTest(lookup(C2, quail),"=",undefined),
   begin associate(CS, take, took),
     associate(CS, keep, kept),
     eqTest(lookup(CS,take),"=",took)
   end,
   eqTest(lookup(CS,keep),"=",kept),
   begin associate(C2, quail, quails),
     associate(C2, duck, ducks),
     associate(C2, owl, owls),
     associate(C2, crow, crows),
     associate(C2, hawk, hawks),
     eqTest(lookup(C2,quail),"=",quails)
   end,
   eqTest(lookup(C2,owl),"=",owls),
   eqTest(lookup(C2,duck),"=",ducks),
   eqTest(lookup(CS,duck),"=",undefined),
   begin associate(CS, take,taking),
     associate(CS, keep,keeping),
     associate(C2, crow, murder),
     associate(C2, quail, covey),
     associate(C2, owl, parliment),
     eqTest(lookup(CS, take), "=", taking)
   end,
   eqTest(lookup(C2,owl), "=", parliment)
  ].
% functions to help with testing, NOT for you to implement
-spec associate(CS::pid(), Key::any(), Value::any()) -> ok.
associate(CS, Key, Value) ->
  CS ! {self(), {associate, Key, Value}},
  receive {CS, ok} -> ok after 1000 -> wrong end.
-spec lookup(CS::pid(), Key::any()) -> any().
lookup(CS, Key) ->
  CS ! {self(), {lookup, Key}},
  receive {CS, {value_is, Value}} -> Value after 1000 -> wrong end.
```

Please write your answer below, completing this module.

`-module(catalogserver).`

6. (20 points) [UseModels] In Erlang, write a “shared variable” server; this server acts like a single variable shared between all the processes in an Erlang program. The server’s state is a value, which can be manipulated by sending the server messages containing functions. These functions transform the server’s state from one value to another. You will write a function `start/1`, which takes an initial value for the state, and creates the server, returning its process id. The server responds to messages of the following forms:

- `{Pid, {run, F}}`, where `Pid` is the process id of the sender, and `F` is a function. The server runs the function by passing it the current state’s value, and obtaining a new state value. The response to this message is of the form `{SPid, {result, NV}}`, where `SPid` is the server’s own process id, and `NV` is the new state value obtained from running `F`. The server continues with `NV` as its new state.
- `{Pid, see}`, where `Pid` is the process id of the sender. The server responds by sending a message of the form `{SPid, Value}` to `Pid` where `SPid` is the server’s own process id and `Value` is the value that is the server’s current state. The server continues with an unchanged state.

The following are tests, written using the homework’s testing module.

```
-module(sharedvarserver_tests).
-import(sharedvarserver,[start/1]).
-import(testing,[dotests/2,eqTest/3]).
-export([main/0, run/2, see/1]).
main() -> dotests("sharedvarserver_tests $Revision: 1.2 $", tests()).
tests() -> compile:file(sharedvarserver),
    S1 = start(0), S2 = start([one]), % make 2 sharedvar servers
    [eqTest(run(S1, fun(X) -> X+1 end),"=",1),
    eqTest(see(S1),"=",1),
    eqTest(run(S1, fun(X) -> X+4 end),"=",5),
    eqTest(run(S1, fun(X) -> X*X end),"=",25),
    eqTest(run(S1, fun(X) -> X*X end),"=",625),
    eqTest(see(S1),"=",625),
    eqTest(see(S2),"=", [one]),
    eqTest(run(S2, fun(Hist) -> [two|Hist] end),"=", [two,one]),
    eqTest(run(S2, fun(Hist) -> [three|Hist] end),"=", [three,two,one]),
    eqTest(see(S2),"=", [three,two,one]),
    eqTest(run(S2, fun(Hist) -> [4|Hist] end),"=", [4,three,two,one]),
    eqTest(run(S2, fun([N|Hist]) -> [N+1|[N|Hist]] end),"=", [5,4,three,two,one]) ].
% functions to help with testing, NOT for you to implement
-spec run(S::pid(), F::fun((State::any()) -> any())) -> any().
run(S, F) ->
    S ! {self(), {run, F}},
    receive {S, {result, Val}} -> Val after 1000 -> wrong end.
-spec see(S::pid()) -> any().
see(S) ->
    S ! {self(), see},
    receive {S, Value} -> Value after 1000 -> wrong end.
```

There is space for your answer on the next page

Please write your answer below, completing the following module.

```
-module(sharedvarserver).
```

7. (20 points) [UseModels] In Erlang, write a “notification” server; this server tracks a list of processes to be notified in case of an event occurring, and supports announcement of such events. The server’s state consists of the name of the event and a list of process ids for the event’s observers. You will write a function `start/1`, which takes the event name (an atom), creates a server for notifying observers about that event, and returns the server’s process id. The server responds to messages of the following forms:

- `{Pid, register}`, which records the process id, `Pid`, as an observer in the server’s state, and responds by sending the message `{SPid, registered}` back to `Pid`, where `SPid` is the server’s own process id.
- `{Pid, observers}`, which sends a message of the form `{SPid, Observers}` to `Pid`, where `SPid` is the server’s own process id, and `Observers` is a list of the process ids of all the registered observers. The state of the server is unchanged.
- `{Pid, announce}`, which notifies each observer in the server’s list of observers by sending it a message of the form `{SPid, {event, EName}}`, where `SPid` is the server’s own process id and `EName` is the name of the event (as given to `start/1`). It then responds by sending the message `{SPid, announced}` back to `Pid`. The server’s state is unchanged.

There are tests below and space for your answer on the next page.

```
-module(notifier_tests).
-import(notifier,[start/1]).
-import(testing,[dotests/2,eqTest/3]).
-export([main/0]).

main() -> compile:file(notifier), dotests("notifier_tests $Revision: 1.3 $", tests()).
tests() -> N1 = start(e1), N2 = start(e2),
    W1 = makeWorker(N1), W2 = makeWorker(N1), W3 = makeWorker(N2),
    lists:foreach(fun(W) -> receive {W, registered} -> ok end end, [W1,W2,W3]),
    [eqTest(observers(N1),"",[W2,W1]), eqTest(observers(N2),"",[W3]),
    eqTest(getCount(W1),"",0), eqTest(getCount(W2),"",0),
    eqTest(getCount(W3),"",0),
    eqTest(begin announce(N1), getCount(W1) end,"",1), eqTest(getCount(W2),"",1),
    eqTest(begin announce(N1), getCount(W1) end,"",2),
    eqTest(getCount(W2),"",2), eqTest(getCount(W3),"",0),
    eqTest(begin announce(N2), getCount(W3) end,"",1), eqTest(getCount(W2),"",2),
    eqTest(begin announce(N1), getCount(W1) end,"",3),
    eqTest(getCount(W2),"",3)
    ].

% functions to help with testing, NOT for you to implement
-spec observers(NS::pid()) -> [pid()].
observers(NS) -> NS ! {self(), observers},
    receive {NS, LOP} -> LOP end.
-spec announce(NS::pid()) -> ok.
announce(NS) -> NS ! {self(), announce},
    receive {NS, announced} -> ok end.

% A worker helps with testing
-spec makeWorker(NSPid::pid()) -> pid().
makeWorker(NSPid) -> TPid = self(),
    spawn(fun() -> workerInit(TPid, NSPid) end).
workerInit(TPid,NSPid) -> NSPid ! {self(), register},
    receive {NSPid, registered} -> TPid ! {self(), registered} end,
    worker(TPid,NSPid,0).

worker(TPid,NSPid,Count) ->
    receive {TPid, count} -> TPid ! {self(), Count},
        worker(TPid,NSPid,Count);
    {NSPid, {event, _EN}} -> worker(TPid, NSPid, Count+1)
end.

getCount(WPid) -> WPid ! {self(), count},
    receive {WPid, Count} -> Count end.
```

Please write your answer below, to complete this module.

`-module(notifier).`